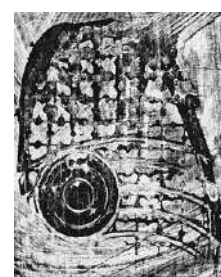
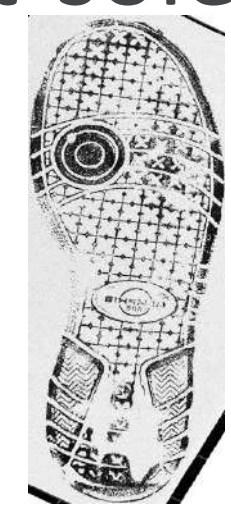


1. Introduction

- The comparison of shoe print images still largely relies on an expert's subjective assessment and experience.
- Crime scene (Q) vs. known out-sole test impression (K).



(A) Partial shoe print
found at crime scene (Q)



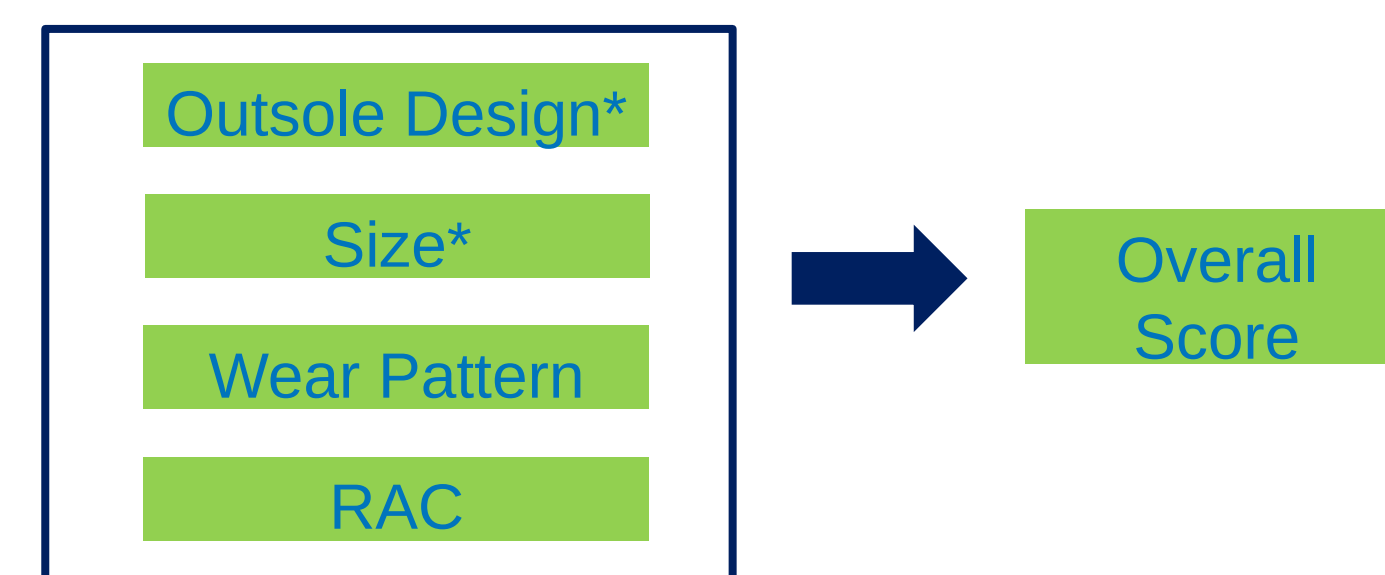
(B) Putative source shoe (K)

- Challenges** : (1) Images lifted from crime scenes are typically partial prints, (2) For comparison, questioned image (Q) and known prints (K) need to be rotated and translated, (3) Images are subject to noise and background effects.

2. Goal

- Goal** : Develop high performing scoring system(s) that quantify the degree of similarity between two out-sole 2D images.

- Contributors to the score :



3. Methods I

- Points of interest** ("data") : Coordinates of all edges (Prewitt operator) and of 500 strong corners (the Harris-Stephens algorithm) in a 2D out-sole image.
- Maximum Clique** (MC) : Largest subset of attributes in one image that is geometrically congruent to a corresponding collection of attributes in the other image. The advantage of using MC is its invariance to rotation and translation.

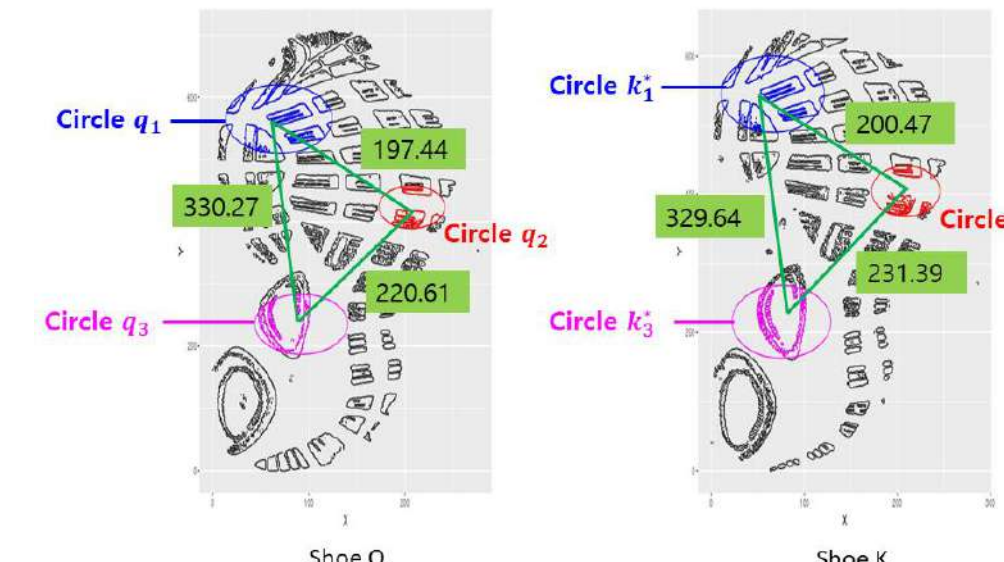
(A) Image1 (B) Image2 (C) Maximum Clique



Figure (A) and (B) are example images. Image 1 has a set of points {a, b, c, d} and image 2 has a set of points {1, 2, 3, 4, 5, 6}. Figure (C) is application of the concept of maximum clique to find the correspondence between image 1 and image 2 is {(a,1), (b,3), (d,6), (c,5)}.

4. Methods II

- Signature of an out-sole image** : We select three semi-arbitrary circular regions and the edge points within.



- Matching** : After alignment of edges in Q and K, fix several circular areas in edges of Q and find the best matching area in K using MC.
- Similarity features** : (1) Clique size, (2) SD of rot. angle, (3) % Overlap on Q, (4) % Overlap on K, (5) Med. Distance of OP, (6) Diff. in triangle Q-K.
- Score** : Multiple similarity features are extracted and combined into single score using a random forest algorithm.

5. Matching Algorithm (MC-SCA)

- Step 1** : Extract edges from shoe Q and shoe K.
- Step 2** : Fix three circles (q_1, q_2, q_3) in "interesting" areas of shoe Q.
- Step 3** : Search over several circular areas in shoe K, and find the circle with highest overlap with circle q_1 .
- Step 4** : From the circle found at step 3, find the corresponding circle k_1^* in shoe K that is best overlap with q_1 in shoe Q.
- Step 5** : Repeat the entire process for at least two additional circles q_2, q_3 in shoe Q and find corresponding k_2^*, k_3^* .

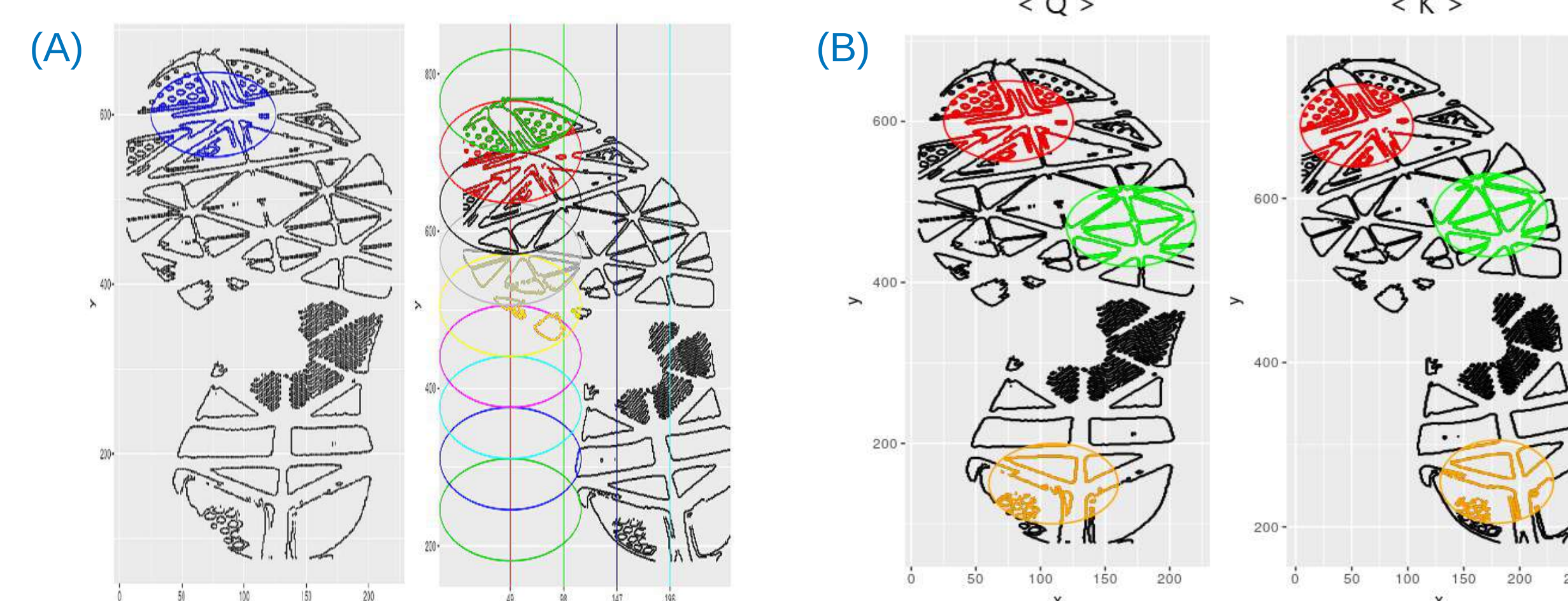


Figure (A) is comparison between shoe Q and shoe K in step 2 and 3. When fixing blue area in shoe Q, many candidate circles are searched over shoe K.

Figure (B) shows a final matching results in step 5. When fixing three sub areas in shoe Q, the corresponding circles in shoe K are found.

6. Data Analysis and results

- Data** : CSAFE obtained replicate 2D images from 38 pairs of NIKE Winflow shoes size 8.5 and 22 pairs size 10.5. Shoes were used for about 6 months.
- Comparisons** : There are 717 known mated (KM) comparisons and 600 known non-mated (KNM) comparisons.

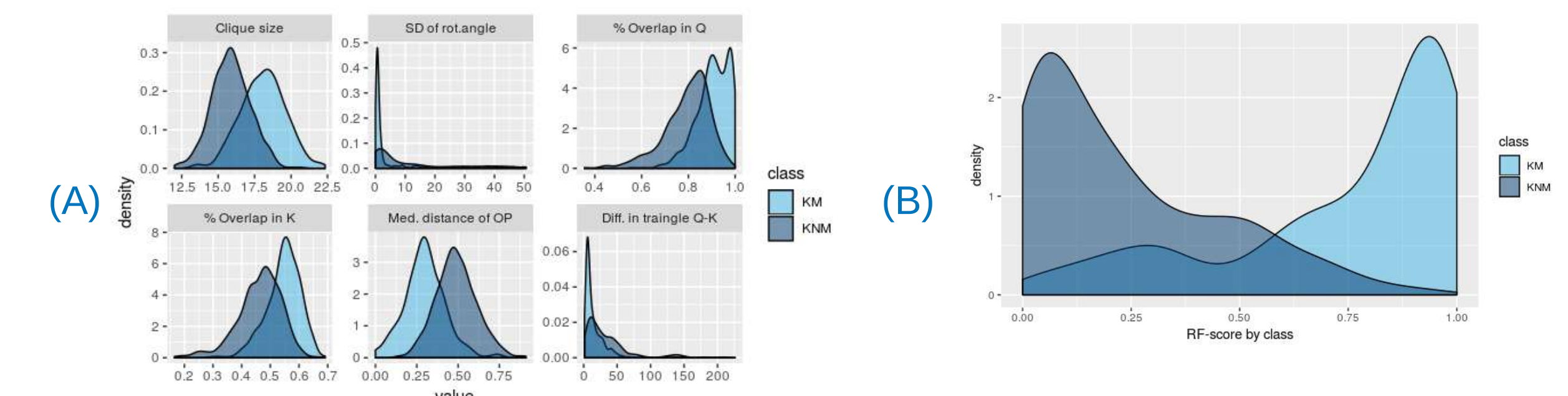
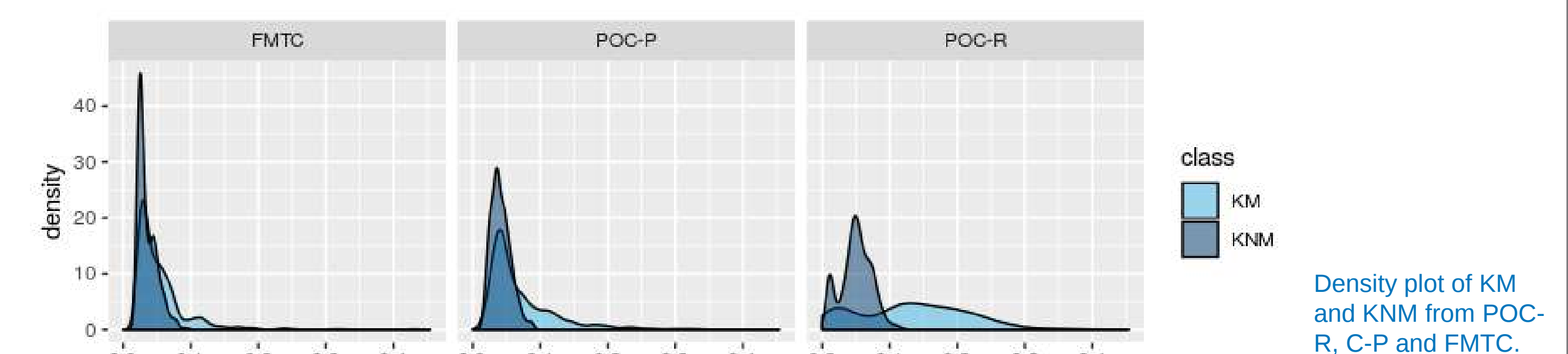


Figure (A) shows densities of class KM and KNM in six similarity features. Figure (B) is a final score predicted by RF on test comparisons.

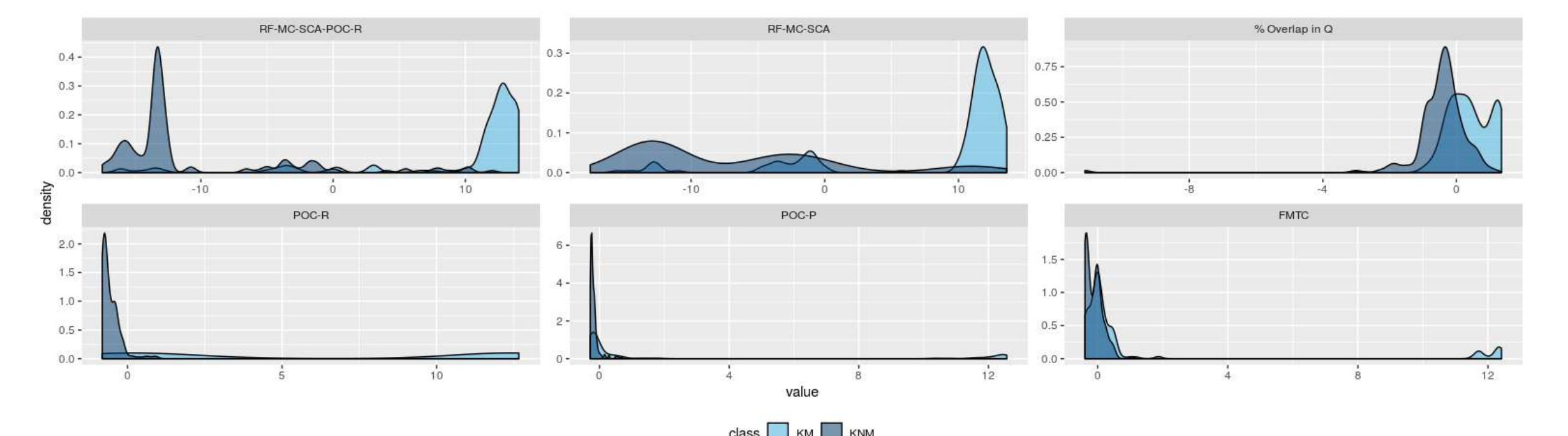
- Methods** : MC-SCA, POC with registration method, POC with principal axis and FMTC.



- Performance on test set** :

Classifiers	AUC	EER
RF-MC-SCA-POC-R	0.970	0.074
RF-MC-SCA	0.907	0.181
% Overlap on Q	0.835	0.246
POC - R	0.796	0.244
POC - P	0.705	0.387
FMTC	0.689	0.387

As a diagnostic tool, ROC curve of six classifiers is drawn. Also, the area under the ROC curve (AUC) and equal error rate (EER) is calculated in the table.



The density of score based likelihood ratio (SLR) in test comparisons is calculated by the training scores. The density of training score in KM and KNM is estimated by kernel density estimation.

7. References

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