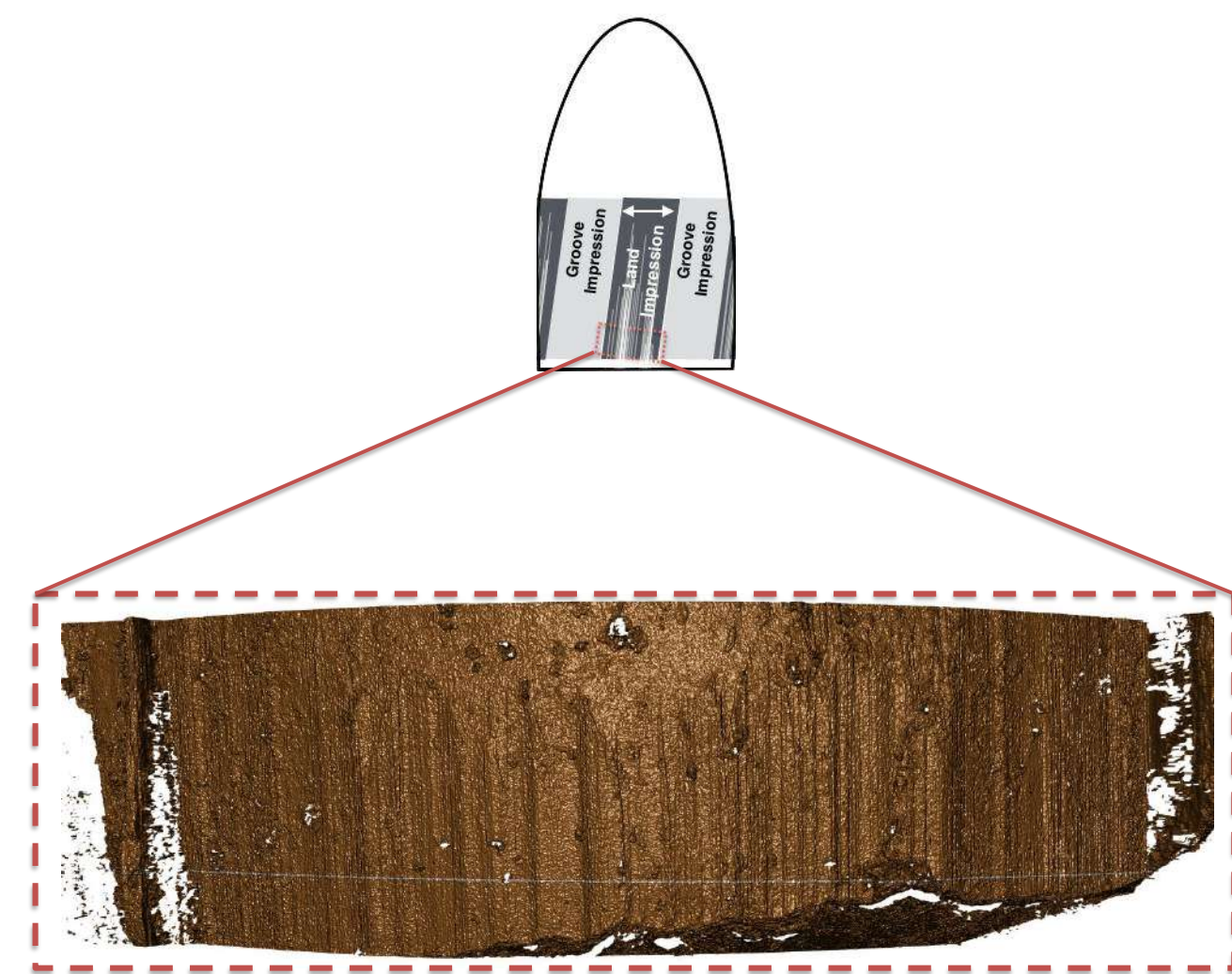


## Background

High resolution 3D microscopy has, in recent years, been the primary technological development which has advanced image-analysis algorithms for automated comparison of bullet **land engraved areas (LEAs)**.



**Figure 1:** An example of a high resolution 3D scan of a bullet land engraved area (LEA). Often, a single bullet will have 6 LEAs in total.

LEA comparison algorithms such as the one developed by Hare et. al. [1] use 2D signatures extracted from 3D scans.



**Figure 2:** The process of extracting 2D data from a 3D scanning object, as Hare et. al. [1] describe.

We designed a **Gauge Repeatability and Reproducibility (Gauge R&R)** study of the high resolution 3D scanning process as it applies to bullet LEAs.

## Data Description

Data presented here are from a pilot study of repeated LEA scans from a Sensofar Confocal Light Microscope:

- Six lands from one barrel (Hamby set 44, Barrel 6) [2]
- Two bullets fired from the same barrel
- Four microscope operators
- Three repetitions per bullet-operator combination

This resulted in 24 scans each for the six **barrel-lands**.

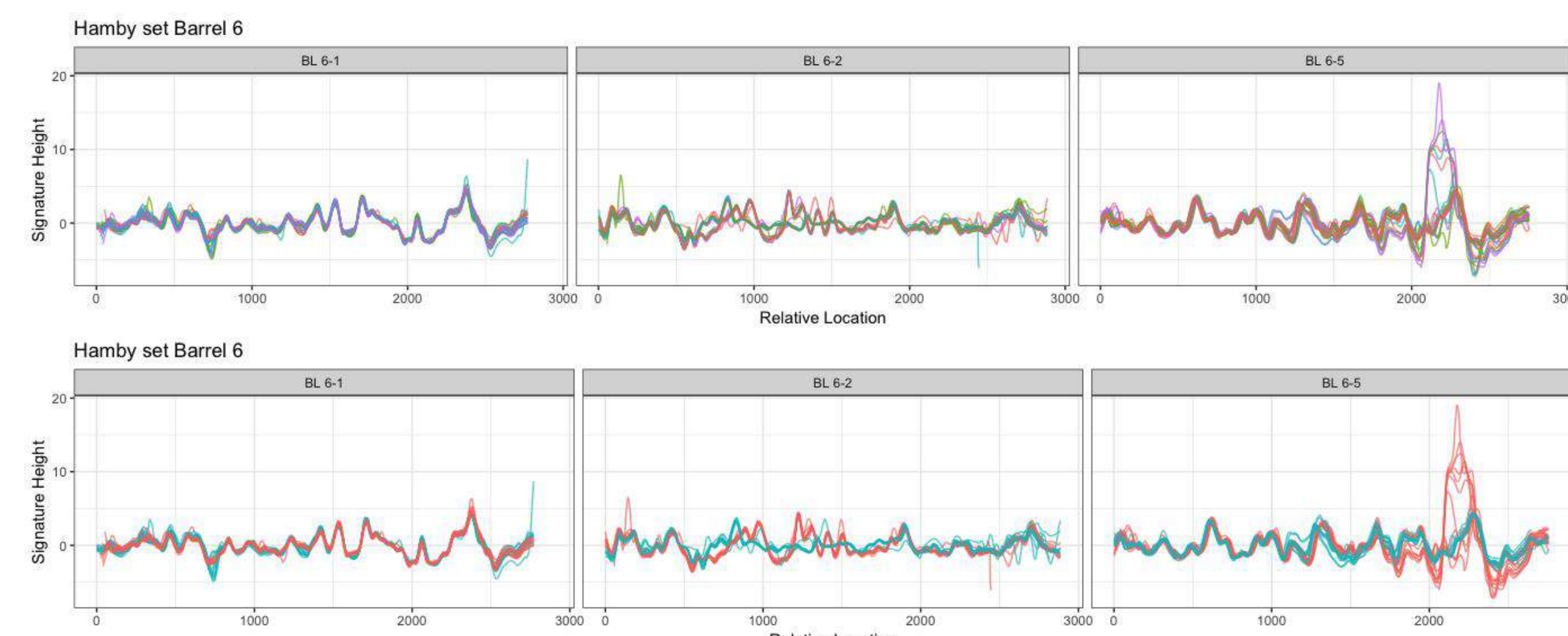
## Data Analysis



**Figure 3:** Two example LEA scans of the same barrel-land from the same bullet.

We investigate variability in the extracted 2D signatures and quantify the impact of differing environmental conditions on pairwise automatic matching scores.

### Extracted Signature Data



**Figure 4:** The characteristics of each individual bullet LEA appear to dominate the signal present due to operator. However, clear operator differences appear for certain LEAs.

### Pairwise Automatic Matching Scores

Do differing environmental conditions have an impact on automated matching?

We fit an effects model derived from traditional R&R on scores from same-source pairings.

$$\begin{aligned} \text{Model 1: } S_{p,p'} &= \text{Random Forest score comparing Signature } p, \text{ Signature } p' \\ &= \mu_{BL} + \beta I[\text{Same Bullet (within source)}] \\ &\quad + \omega I[\text{Same Operator}] + \beta \omega I[\text{Same Bullet and Operator}] \\ &\quad + \epsilon \end{aligned}$$

| Description                            | Parameter              | Estimate |
|----------------------------------------|------------------------|----------|
| Fixed mean for Barrel 6-Land 1         | $\mu_{6-1}$            | 0.997    |
| ⋮                                      | $\mu_{6-2}$            | 0.821    |
| ⋮                                      | $\mu_{6-3}$            | 0.995    |
| ⋮                                      | $\mu_{6-4}$            | 0.976    |
| ⋮                                      | $\mu_{6-5}$            | 0.895    |
| Fixed mean for Barrel 6-Land 6         | $\mu_{6-6}$            | 0.999    |
| Same bullet random effect              | $\sigma_{\beta}$       | 0.090    |
| Same operator random effect            | $\sigma_{\omega}$      | 0.00001  |
| Bullet-operator interaction rand. eff. | $\sigma_{\beta\omega}$ | 0.000    |
| Residual error                         | $\sigma$               | 0.118    |

**Table 1:** The estimated parameters from Model 1. Operator variability is minimal, and mean scores for Barrel-Lands 6-2 and 6-5 are lower than the others.

## Pilot Study Insights

1. The biggest differences in pairwise automatic matching scores are due to:

- individual bullet characteristics
- breakoff
- operator capture of breakoff

2. Future work should focus on:

- microscope differences
- multiple barrel types
- three bullets per barrel
- developing a framework for reproducibility studies

## Future Data Collection

We are in the process of collecting an expanded set of scanning variability data:

- Six lands each from three barrel types  
Hamby set 224  
Houston  
CSAFE Persistence
- Three bullets fired from each barrel
- Five microscope operators
- Two Sensofar Confocal Light microscopes
- At least three repetitions per bullet-operator-machine combination

This will result in at least 90 scans for each barrel-land.

## References

- [1] Hare, E., Hofmann, H., and Carriquiry, A. (2016). Automatic matching of bullet land impressions. *The Annals of Applied Statistics*, 11:2332-2356.
- [2] Hamby J. E., Brundage D. J., Thorpe J. W. (2009). The identification of bullets fired from 10 consecutively rifled 9mm Ruger pistol barrels: A research project involving 507 participants from 20 countries. *AFTE Journal*, 41(2):99-110.